Abstract: To provide broad band connectivity to the mobile users and to build a self-structured network, where it is not possible to have wired network, “Wireless Mesh Networks” are the most vital suitable technology. Routing in Wireless Mesh Networks is a multi-objective nonlinear optimization problem with some constraints. We explore multicast routing for least-cost, delay-sensitive and congestion-sensitive in optimizing the routing in Wireless mesh networks (WMNs). In this work different parameters are associated like edge cost, edge delay and edge congestion. The aim is to create a tree traversing which the set of target nodes are spanned, so as to make the cost and congestion to be minimum with a bounded delay over the path between every pair of source and destination. Since searching optimal routing satisfying multiple constraints concurrently is an NP complete problem, we have presented a competent estimated algorithm certified with experimental results, which shows that the performance of presented algorithm is nearly optimum.

Keywords: Wireless Mesh Networks, Routing protocol, traffic, Congestion, delay bound.

1. Introduction

In order to broadband access over Internet and to share network resources by civic and organization consumers, wireless mesh networks (WMNs) delivers a cost effective way that uses multi-hop networking technique[1,2,3]. Intermediary hops in the mesh networks of WMNs complete the routing by passing data from point to point by using forwarding decisions and also boost the signal. WMNs have numerous benefits, such as small scalable, robustness,[4] hassle-free network maintenance, consistent service etc. Recently quite a lot of evolving networks applications built on WMNs architecture have been set up. For instance, the Portsmouth Real-time Travel Information (PORTAL) - ambitions at providing real-time travel information to the customers [5]. One more application is in civic security, which in order to offer mobility support, consistently, with flexibility, and high bandwidth, adds demand for wireless network connectivity. As WMNs mainly provides broadband services satisfying heterogeneous QoS desires. Therefore QoS is one of the most basic requirements and in case of WMNs this is the highly constraints requirements of a user. For the improvement of QoS in WMNs different changes has been done in routing protocols of WMNs. The network topology in WMNs varying constantly. Many trees are used in Mesh based network protocols, to facilitate the delivery of the packets to every receiver via distinct paths. Existence of multiple path increases the protections against the topology changes. There is different scenario for multicast in WMNs. In our approach we assume that each access point sends it’s traffic flow to more than one mesh router i.e. we can say it’s a type of multicasting host in routing the flows from source to destination gateway mesh router with the following optimization goal: delay optimization, cost optimization and congestion optimization. This paper aims at finding the optimal multicast route in wireless mesh networks fulfilling the issues:- minimum congestion, endwise delay constraint is fulfilled, least cost. An optimal MCMT is a tree originated at some source node \( s \) that covers the destinations node set \( S \) and the total delays along the route between the source \( s \) and every destination \( \sigma \in S \) is restricted and is not exceeded by delay constant \( D \) and sum total of the cost over the links in the tree spanning the destinations is minimum and such that each edge used must satisfies the congestion constraint described. In the experimental and result part we have discussed, the efficiency of MCMT which consider three parameters cost, delay bound and congestion is more closer to the optimal solution compared to modified KMB [6].

2. Literature review

Routing in WMNs is a vital in the performance evaluation of wireless mesh network. A lot of analysis has been conducted for the development of routing scheme that can optimize the throughput of WMNs whereas satisfying different matrices. In earlier optimization technique network delay and cost optimization are been the two important optimization goals taken into consideration as distinct problem in multicast routing. Delay optimization is described as follows. The optimum delay solution in a WMNs modeled as \( G=<V,E> \) where vertices set \( V \) denotes mesh nodes and \( E \) denotes the links in the network so that the total amount of delays in the route between source and destinations becomes minimum. Dijkstra's shortest path algorithm [7] can be used to create the shortest route between the source and target nodes which offers the optimal result for optimization of delay. Optimizing the cost in WMNs modeled by a graph \( G=<V,E> \) where vertices set \( V \) represents a mesh node and \( E \) represents the set of communication link in the network, is defined as follows. Cost is a function \( C:E\rightarrow R^+ \) such that \( C(e)=b+ve \) real constant, optimizing the cost in multicast rout means to construct a tree, that covers the destinations in such a way that the total cost over the edges in the tree becomes minimum. Also, this is known as Steiner tree problem[8] and NP complete[9]. Still, Steiner tree problem have been solved using some heuristics approach that take polynomial time [10,11,12] and yield nearly optimum outcomes. Wall[13] deliver how to generate the multicast tree using Steiner tree algorithm proposed by Kou, Markowsky and Berman. Waxman[14] investigated on the idea of modification of the tree in the case of nodes joining or leaving the tree dynamically. Chow[15] viewed at the
multiparty connections problem from two approaches. First, designing the multicast route whose computation time is least. And then, multiple communications are combined into one route. Optimization on both cost and delay[16] was only addressed by Kabda and Jaffe taking both as identical function and their results becomes false if the two functions are different. Verma and Ferrari [17] design a process to construct path that account for constraint delay in unicast networks. Kompella Pasquale and Polyzos [18] discussed the optimization of multicast routing taking both cost and bounded delay as a matrices. Rakesh Matam and Somanath Tripathy[19] discusses Multicast Routing in WMNs. Khalid Mahmood, Babar Nazir, Iftikhar Ahmad Khan and Nadir Shah [20] studied the existing cost metrics and proposed a genetic algorithm technique for routing in WMN. Ahmed Al-Saadi, Rossitza Setchi and Yulia Hicks [21] discusses a new heterogeneous routing protocol and a routing algorithm based on reinforcement learning called cognitive heterogeneous routing are proposed to select the appropriate transmission technology based on parameters from each network. The proposed heterogeneous network overcomes the problems of sending packets over long paths, island nodes, and interference in WMNs and increases the overall capacity of the combined network by utilizing unlicensed frequency bands instead of buying more license frequency bands for LTE. Celso Barbosa Carvalho and José Ferreira de Rezende [22] discusses WMNs scenarios with routers able to adapt communication channel width; therefore, we propose a metric implemented in the network layer in order to increase the end-to-end capacity of routes, and consequently increase the network capacity. Metric values are used to establish the routing flows; conduct channel assignment, select the width of each channel and choose, due to the existing interference, the amount of transmission radios used in each link. 

Here our aim is to construct a tree rooted at the source s spanned over the destination set S considering cost, bounded delay and congestion as the matrices. This paper is organized as follows: In section-3 we give a proper statement of the Multi Constraint Multicast Tree problem and specify the technique which we use for problem solving. Section-4 describes the pseudo code for MCMT algorithm. Section-5 describes experiments for the performance evaluation of the algorithm. The results of the experiments are discussed in Section-6 and section-7 describes the conclusions.

### 3. Multicast Scenario in Wireless Mesh Networks

In WMNs, a high speed routers equipped with advance antennas forms a mesh backbone and these mesh routers backbone is connected to the internet using access point which are considered as traffic control gateway gates between internet and WMNs. These control gates are known as gateway. In WMNs the sender and receiver for a multicast group are the internet host and mesh host.

**Sender Mesh host, Receiver or access point Internet host:**
In this case the sender uses access point its serving access point. The source sends data to access point which in-turn multicast these data to the receivers. Here access point is again a receiver in this multicast group which receives the data from receivers and sends it back to the sender.

**Sender Mesh Host, Receiver Mesh Host:**
In this case it is needed to first build a multicast routing tree with sender as the source node. The sender first sends a message to the concern access point to give the information about the Group ID and its IP. The form request will be sent be receiver to its related access point which has the multicast group ID. Access point responds to the message and informs the receiver about the sender’s IP address. After getting the IP address of the sender, from the access point, the receiver runs the SPTM protocol to construct a route from the sender to the receiver.

**Sender Internet Host, Receiver Mesh Host:**
In this framework first the mesh host sends a join request to the connected access point. It sends an acknowledgement to the mesh host that it is ready to be the root of the multicast tree in the backbone. Then two senders begin to send the data to the access point which in turn multi casted by the access point using established multicast tree.

Therefore multicast routing is the most critical point in WMNs and needs to be optimized. Based on the founding optimal solution the multicast routing has been classified into 3 groups:

1. Heuristic optimization algorithm.

Generally multicast routing algorithms have been studied developed using heuristic method. Our aim is to design a routing technique that optimizes the traffic flow from the access point to the gateway in WMNs. In our approach we assume that each access point sends it’s traffic flow to more than one mesh router i.e. we can say it’s a type of multicasting host in routing the flows from source to destination gateway mesh router it must consider the following optimization goal:

1. Delay optimization
2. Cost optimization

**Delay optimization:**

Here mesh network is modeled as a graph $G = (\mathcal{V}, \mathcal{E})$ where the vertices set $\mathcal{V}$ represent mesh nodes and the edge set $\mathcal{E}$ represents communication links in the network. Delay is a function $\delta : \mathcal{E} \rightarrow R^+$ such that $\delta(e) = a$ is a positive constant. Optimizing the delay means, minimizing the sum total of all the delays over the links in the route between source and destination.

**Cost optimization:**

Here mesh network is modeled as a graph $G = (\mathcal{V}, \mathcal{E})$ where the vertices set $\mathcal{V}$ represent mesh nodes and the edge set $\mathcal{E}$ represents communication links in the network. Cost is a function $\zeta : \mathcal{E} \rightarrow R^+$ such that $\zeta(e) = b + a$ where $a$ is a real constant. Optimizing the cost means minimizing the sum total of cost over the edges in the tree spanning the destination set.

**Congestion optimization:**

Here mesh network is modeled as a graph $G = (\mathcal{V}, \mathcal{E})$ where the vertices set $\mathcal{V}$ represent mesh nodes and the edge set $\mathcal{E}$ represents communication links in the network. Congestion is the ratio of the flow on the edge to the capacity of the edge i.e. congestion is a function $\zeta : \mathcal{E} \rightarrow [0, 1]$ such that $0 \leq \zeta(e) \leq 1$. Optimizing the congestion means choose the edge in the path only if it’s congestion value is less than one if it is one, that edge is not included in the path.
Multi Constraint Multicast Tree Problem (MCMT):
The Multi Constraint Multicast Tree Problem is given below: The graph \( G \) represents a mesh network with the above described Delay, Cost and Congestion Optimization goal.

In the above defined graph the multicast is defined using following five factors: a source node, a target node set \( \mathcal{S} \), a delay constraint function \( \mathcal{D} \), a cost function \( \mathcal{C} \) and a congestion function \( \mathcal{K} \). An optimal MCMT is a tree originated at \( \mathcal{S} \) that covers the destinations set \( \mathcal{D} \) and the total delays along the route between the source \( \mathcal{S} \) and every destination \( \mathcal{D} \in \mathcal{D} \) is restricted and is not exceeded by \( \mathcal{D} \) and sum total of the cost over the links in the tree spanning the destinations is minimum and such that each edge used must satisfies the congestion constraint described above.

4. The Definition of Multi Constraint Multi Cast Routing

4.1 Network and interference model

The wireless mesh network model which we have considered is represented hierarchically, in which the data from mobile clients aggregated at the local access points which in turn communicate with the mesh router forming the mesh backbone which in turn forward it to the gateway access point which is connected to the Internet. Here mesh nodes are the gateway access point, mesh routers and local access point.

The mathematical model of the described mesh network is as follows. The entire mesh network is modeled as a graph \( G = (\mathcal{V}, \mathcal{E}) \) such that \( \forall v \in \mathcal{V} \) represent the mesh node and some of nodes \( g \in \mathcal{V} \) is the gateway access point connecting to the Internet via wired connection. In the graph an edge \( e = (u, v) \in \mathcal{E} \) represent that the mesh node represented by \( u \) can transmit the mesh node represented by \( v \) directly without an intermediate node. Here we have taken assumption that the transmission range \( R_u \) and the interference range \( R_{ii} = (1 + \delta) R_u \) where \( \delta \geq 0 \) is a constant, for every mesh node is uniform. \( (u, v) \in \mathcal{E} \) represents the distance between the nodes \( u \) and \( v \). An edge \( e = (u, v) \in \mathcal{E} \) exist if \( e < u, v \geq R_{ii} \). The edge length is represented by \( e(e) \) and the capacity of the edge is represented as \( c(e) \) i.e. a maximum of \( c(e) \) bits can be carried in one second by the edge. The congestion function \( \mathcal{K}(e) \) is the ratio of the flow over the edge to its capacity i.e. \( \mathcal{K}(e) = \frac{\delta(e)}{c(e)} \) where \( \delta(e) \) represent the flow over the edge and \( c(e) \) is the capacity of the edge.

4.2 Problem Formulation

This paper aims at finding the optimal multicast route in wireless mesh networks fulfilling the issues:-

1. Minimum congestion
2. Endwise delay constraint is fulfilled
3. least cost.

The Multi Constraint Multicast Tree is defined as follows. Mesh backbone network is modeled as a graph \( G = (\mathcal{V}, \mathcal{E}) \) with a cost function \( \mathcal{C} : \mathcal{E} \rightarrow \mathbb{R}^+ \) and a delay function \( \mathcal{D} : \mathcal{E} \rightarrow \mathbb{R}^+ \) and a congestion function \( \mathcal{K} : \mathcal{E} \rightarrow [0,1] \) such that \( 0 \leq \mathcal{K}(e) \leq 1 \) is a congestion function. In order to express the problem some earlier explanations are needed. In the above defined graph the multicast is described using following five parameters: a source node \( \mathcal{S} \), a target node set \( \mathcal{D} \), a delay constraint function \( \mathcal{D} \), a cost function \( \mathcal{C} \) and a congestion function \( \mathcal{K} \). An optimal MCMT is a tree originated at \( \mathcal{S} \) that covers the destinations set \( \mathcal{D} \) and the total delays along the route between the source \( \mathcal{S} \) and every destination \( \mathcal{D} \in \mathcal{D} \) is restricted and is not exceeded by \( \mathcal{D} \) and sum total of the cost over the links in the tree spanning the destinations is minimum and such that each edge used must satisfies the congestion constraint described above.

The above MCMT is NP-complete but here we have written heuristic algorithm to construct a solution which is approximately optimal and is built on approximation algorithm of Steiner tree by Berman, Kou, and Markowsy[23].

First the KMB algorithm is described and demonstrated in figure-1 where all the edges in the graph are assumed to be of cost and delay of unit amount. The destination node set to be covered is \( \{V, Y\} \) with \( U \) as the source.

**Figure 1.** The KMB algorithm. (a) The graph. (b) The MST. (d) The Spanned tree.

**STEP I:**
\( G \) is a given graph as in (figure-1.a). A complete graph \( G' \) on the set \( S \cup \{S\} \) is constructed such that \( (x, y) \in G' \) is the path with least cost between node \( x \) and \( y \) (figure-1.b).

**STEP II:**
From \( G' \) a minimum spanning tree \( T \) is constructed (figure-1.c).

**STEP III:**
The links in \( T \) are then extended to the edges in \( G \), that set up the least cost path of \( G' \) (figure-1.d).

The above KMB algorithm does not essentially yield a MCMT. But, we have added constraints at every step which guarantee that it produces an MCMT.
path subjected to the delay of the path being less than \( D \) such that each edge in the path must obey the congestion constraint. Suppose \( C(p, q) \) be the cost on the edge \( (p, q) \), \( \alpha(e) \) be the delay and \( \alpha(e) \) where \( e = (p, q) \) be the congestion over the \( (p, q) \). \( C_d(p, q) \) be the cost of shortest path between \( p \) and \( q \) having delay \( d \).

\[
C_d(p, q) = \min_{z \in S} C_d - \alpha(z) + C(z, q) \text{ and } C(p, q) = \min_{0 \leq d \leq D} C_d(p, q)
\]

Below we have describe MCMT algorithm and applied on the identical graph as in figure-1.

**Figure 2.** The MCMT algorithm. (a) The graph. (b) The closure graph. (c) The MST. (d) The constrained multicast tree.

**STEP I:**

G is a given graph as in (figure-2.a). A complete graph \( G' \) on the set \( S \cup \{s\} \) is constructed such that \( < p, q > \in G \) is the path with least cost between node \( p \) and \( q \) (figure-2.b). The path delay, path cost and congestion is represented on the links in the graph.

**STEP II:**

A constrained minimum spanning tree \( T \) of \( G' \) (figure-2.c) using Prims technique [24] is constructed, with the following critical measure \( C_n \) and congestion factor \( f \) that decides the particular edge is added or subtracted at every iteration.

\[
C_n = \left\{ \begin{array}{ll}
C(p, q) & \text{if } \partial_p(p) + \partial'(p, q) < D \\
\infty & \text{otherwise}
\end{array} \right.
\]

where \( \partial_p(p) = \text{delay along the path from } p \) to \( p \) \( \partial'(p, q) = \text{delay along the shortest constraint route between } p \) and \( q \) \( f = \frac{\partial'(p, q)}{\text{Capacity}(p, q)} \) where \( \beta(x, y) = \text{flow on the edge } (p, q) \) and \( \text{Capacity}(p, q) = \text{total traffic that edge } (p, q) \text{can carry}. \)

**STEP III:**

The links in \( T \) are then extended to the edges in \( G \), that set up the route with least cost in \( G' \) (figure-2.d).

In the above algorithm the critical measures balance is the selection of the edge with least cost against its delay leftover. The probability that same route can be used for data sending depends on the residual delay i.e. the delay leftover.

/* **Pseudo code for MCMT algorithm** */

*input: network topology
*output: set containing all the *destination nodes with source
\* \( G = (V, E) = \text{mesh network topology} \)
*model
\* \( s = \text{source node} \)
\* \( S = \text{destination set} \)
\* \( D = \text{delay bound} \)
*/

\[
MCMT(G, s, S, D)
\]

\{
\* */
\* it is assumed that cheapest constraint path have * been found between all nodes and is represented
\* by \( V' \)
\* *
\* \( V' = S \cup \{s\} \)
\* for every edge \( <p, q> \in V' \)
\* \( C(p, q) = \text{cheapest} \)
\* constrained path cost between \( p \) and \( q \);
\* \( \partial[p, q] = \text{cheapest} \)
\* constrained path delay between \( p \) and \( q \);
\* \( \delta[p, q] = \text{traffic flow on edge} \)
\* along the route between \( p \) and \( q \);
\* }

\[
C = \{s\};
\* \( P[s] = 0; \)
*/

\* till every node in \( V' \) have been covered
*
*/

while(\( C \neq V' \))
\{
\* min = \infty
\* for every \( p \in C \)
\* 
\* for each \( q \in V' - C \)
\* 
\* if(\( C_m(p, q) < \infty \& \& \partial[p, q] + \) \( P[p] < D \& \& f < 1 \))
\* 
\* \( \text{nextedge} = (p, q) \); 
\* \( \text{min} = C_m(p, q) \); 
\* \( u = q; \)
\* 
\* \( C = C \cup \{u\}; \)
\* \( P[u] = P[p] + \partial[p, q]; \)
\* 
\* 
\*
\}
5. Experiments and Results

To determine the average case performance of MCMT algorithm is ran on a number of graphs generated randomly. The optimum solution is first found by computing all constrained spanning tree and selecting the tree with least cost. Then using MCMT heuristic algorithm a constraint multicast tree is generated. At last we formed constrained spanning tree thru arbitrarily selecting edges till solution was obtained. Then the cost is compared in all of the above three cases in terms of two measures—

i. **Average normalized distances** - average normalized distances represented by \( \gamma \), and

\[
\gamma = \frac{1}{n} \sum_{j=1}^{n} \frac{X_j - O_j}{O_j}
\]

where \( X_j = \text{cost of MCMT in } j_{th} \text{ run} \)
and \( O_j = \text{cost of Optimal Tree in } j_{th} \text{ run} \)

The average normalized distance indicate percentage, above the optimal cost incurred using MCMT. Less the percentage of average normalized distance better the performance of the algorithm.

ii. **Efficiency** \( (\tau) \) – efficiency is a measure which is used to rank MCMT algorithm stuck between the optimal solution(best) and random solution(worst) performances.

\[
\tau = \frac{\sqrt{\frac{1}{n} \sum_{j=1}^{n} (A_j - X_j)^2}}{\sqrt{\frac{1}{n} \sum_{j=1}^{n} (A_j - O_j)^2}}
\]

where \( A_j = \text{cost of arbitrary tree in } j_{th} \text{ run} \)
\( X_j = \text{cost of MCMT in } j_{th} \text{ run} \)
\( O_j = \text{cost of Optimal Tree in } j_{th} \text{ run} \)

A number of diverse sized graphs were tried. The factors based on which the graphs are generated are given below—

Each graph must have at least one solution. The degree of each node in the graph must be between 1 and a maximum value. Every edge had a cost of one unit and associated with a delay of a random value from the set \( \{1, 2, \ldots, 10\} \). Several destination set of different sizes were considered. Different delay constraints were also tried. The different parameters for the experiment are given in table 1.

<table>
<thead>
<tr>
<th>Table 1. Experimental Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>No. of Runs</strong></td>
</tr>
<tr>
<td><strong>No. of Nodes</strong></td>
</tr>
<tr>
<td><strong>Maximum Node Degree</strong></td>
</tr>
<tr>
<td><strong>Destination Set Dimension</strong></td>
</tr>
<tr>
<td><strong>Cost of Edge</strong> ( (e) )</td>
</tr>
<tr>
<td><strong>Delay on Edge</strong> ( (e) )</td>
</tr>
<tr>
<td><strong>Delay Bound Constraint</strong></td>
</tr>
</tbody>
</table>

We have set up an irrepressible forwarding mesh network approach that protects a multicast session in wireless mesh networks. In a multicast session in irrepressible forwarding mesh network every source-destination pair has at least two node disjoint path connecting the source and destination simultaneously. Because of which failure of any intermediate node or a single link in an irrepressible forwarding mesh network won’t interrupt the multicast session. The following small network topology given in figure 3(a) demonstrate the concept of irrepressible forwarding mesh network. In the given example there is one source node represented by \( s \), three intermediate nodes represented by \( N1, N2 \) and \( N3 \), and two destination nodes represented by \( d1 \) and \( d2 \). Here as both \( N1 \) and \( N2 \) are in the transmission range of \( s \) only one broadcast transmission from \( s \) is sufficient for nodes \( 1 \) and \( 2 \). Successively the packets are further broadcasted to \( d1 \) and \( N3 \) by \( N1 \) and to \( d2 \) and \( N3 \) by \( N2 \) and to \( d1 \) and \( d2 \) by \( N3 \). The above given four broadcast transmission establishes an irrepressible forwarding mesh network comprises two node disjoint route for every source destination pair as given in figure 3(b). In the given example \( \{s, d1\} \) is linked by both \( s \rightarrow N1 \rightarrow d1 \) and \( s \rightarrow N2 \rightarrow N3 \rightarrow d1 \) and \( \{s, d2\} \) is linked by both \( s \rightarrow N2 \rightarrow d2 \) and \( s \rightarrow N1 \rightarrow N3 \rightarrow d2 \) as shown in figure 3(c).

![Figure 3. Irrepressible forwarding mesh](image)

In figure 4 the thick lines shows the efficiency of modified KMB algorithm with two matrices cost and delay bound [25,26] while the dotted lines shows the efficiency of MCMT which consider three parameters cost, delay bound and congestion which is more closer to one i.e. more closer to the optimal solution compared to modified KMB [26]. We also observed that the efficiency is inversely related to the delay. In figure 5 we observed that efficiency is inversely proportional to the number of nodes but the efficiency decrease at a less rate with the increase in number of nodes in MCMT as shown by dotted lines. Finally we plotted the graph figure 6 of average normalized distance vs number of nodes and we found that average normalized distance increases with the number of nodes but at less rate in MCMT as compare to modified KMB algorithm with two matrices cost and delay bound[26]. In all of the above case the delay is bounded above by 20units.In figure 7 shows the drops in efficiency incase if the node failure occurs. The drops in efficiency is lesser in proposed case where irrepressible forwarding mesh network approach is taken but the delay in dropping of the packets to the destination is increased to a significant level which is shown in the figure 8.
6. Conclusions

Searching for the optimum route satisfying multi constraint concurrently in wireless mesh network is an NP complete problem. We have considered the multicasting problem with the constraints cost, delay and congestion. Here one source routing based solution has been assumed. The cost of multicast is minimized with guaranteeing the delay in between source and destination and with the edges in the path has least congestion in the proposed MCMT algorithm. The result shows that this exploratory algorithm has good performance when compared with the optimal solution. Since the mobile nodes have some limitations such as inadequate power, if it has multicast requirements, it simply directed the requirements to its neighboring mesh router which search an optimum path and then sent the path to the source node. Our future interests are to expand the competence by adding more new matrices.

References


